

# Current Trends in Argumentation Dynamics

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# Who am I? What do I do?



Me, at KR'23 in Rhodes



Toulouse

- 2012-15: PhD in Computer Science
  - 2015-16: Postdoc at TU Wien
  - 2016-24: Associate Professor at Université Paris Cité
  - 2024-...: Junior Professor at Université Toulouse Capitole
- Knowledge representation and reasoning
    - Somewhere between formal logic and computer engineering
  - More precisely, argumentation
    - Connections to AAMAS

- Ask questions during the talk
- Ask questions after the talk (`jean-guy.mailly@irit.fr`)
- Stay in touch :)
  - <https://www.linkedin.com/in/jeanguymailly/>

## How to get the slides?

[https://jgmailly.github.io/assets/pdf/EASSS2024\\_Mailly.pdf](https://jgmailly.github.io/assets/pdf/EASSS2024_Mailly.pdf)



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Introduction to Abstract Argumentation

Dung's Framework

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# What is Argumentation?

- Argumentation is an important part of human reasoning
  - Justifying one's own beliefs/decisions
  - Convincing someone else to believe something/do something
  - Analysing conflicting pieces of information
- Formal argumentation in AI studies:
  - Modeling of arguments and their relationships
  - Acceptability of arguments
  - Protocols for several agents using arguments in dialogues
- Two families of formal models
  - Structured/logic-based frameworks
  - Abstract frameworks

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## Dung's Abstract Argumentation Framework

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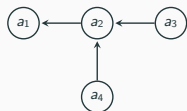
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$F = \langle A, R \rangle$  with

$A = \{a_1, a_2, a_3, a_4\}$ ,

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P. M. Dung: On the Acceptability of Arguments and its Fundamental Role in Nonmonotonic Reasoning, Logic Programming and n-Person Games. *Artif. Intell.* 77(2): 321-358 (1995)

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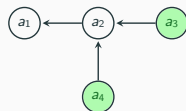
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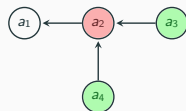
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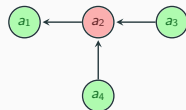
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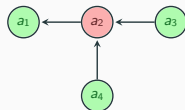
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- It doesn't work if there are cycles  $\rightarrow$  various semantics to remedy this issue

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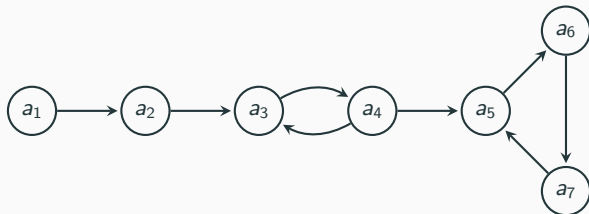
## Extension-based Semantics

Given  $F = \langle A, R \rangle$ ,  $S \subseteq A$  is

- *conflict-free* (**cf**) if there is no  $a, b \in S$  s.t.  $(a, b) \in R$
- *admissible* (**ad**) if  $S \in \mathbf{cf}(F)$  and  $S$  defends all its elements
- *stable* (**st**) if  $S \in \mathbf{cf}(F)$  and  $S$  attacks each argument in  $A \setminus S$
- *complete* (**co**) if  $S \in \mathbf{ad}(F)$  and  $S$  doesn't defend any argument in  $A \setminus S$
- *preferred* (**pr**) if  $S$  is  $\subseteq$ -maximal in  $\mathbf{ad}(F)$
- *grounded* (**gr**) if  $S$  is  $\subseteq$ -minimal in  $\mathbf{co}(F)$

P. M. Dung: On the Acceptability of Arguments and its Fundamental Role in Nonmonotonic Reasoning, Logic Programming and n-Person Games. Artif. Intell. 77(2): 321-358 (1995)

## Example: Semantics Comparison

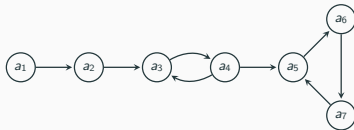


Semantics $\sigma$	$\sigma$ -extensions	$cred_{\sigma}$	$skep_{\sigma}$
grounded	$\{\{a_1\}\}$	$\{a_1\}$	$\{a_1\}$
stable	$\{\{a_1, a_4, a_6\}\}$	$\{a_1, a_4, a_6\}$	$\{a_1, a_4, a_6\}$
preferred	$\{\{a_1, a_4, a_6\}, \{a_1, a_3\}\}$	$\{a_1, a_3, a_4, a_6\}$	$\{a_1\}$
complete	$\{\{a_1, a_4, a_6\}, \{a_1, a_3\}, \{a_1\}\}$	$\{a_1, a_3, a_4, a_6\}$	$\{a_1\}$

- $cred_{\sigma}(F) = \cup_{S \in \sigma(F)} S$ : credulously accepted arguments
- $skep_{\sigma}(F) = \cap_{S \in \sigma(F)} S$ : skeptically accepted arguments

- 3-valued representation of extensions
- Given  $F = \langle A, R \rangle$  an AF, and  $S$  a  $\sigma$ -extension,
  - $L_S(a) = \text{IN}$  iff  $a \in S$ ,
  - $L_S(a) = \text{OUT}$  iff  $\exists b \in S$  s.t.  $(b, a) \in R$ ,
  - $L_S(a) = \text{UNDEC}$  otherwise

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Semantics $\sigma$	$\sigma$ -labellings
grounded	$\{\{a_1, a_2, a_3, a_3, a_5, a_6, a_7\}\}$
stable	$\{\{a_1, a_2, a_3, a_4, a_5, a_6, a_7\}\}$
preferred	$\{\{a_1, a_2, a_3, a_4, a_5, a_6, a_7\}, \{a_1, a_2, a_3, a_4, a_5, a_6, a_7\}\}$
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<https://pyarg.npai.science.uu.nl>

The screenshot shows the PyArg website interface. At the top, there is a blue navigation bar with the text "PyArg" on the left and a series of menu items: "Generate", "Visualise", "Learn", "Algorithms", and "Applications", each followed by a downward arrow. To the right of these items is a "Colorblind mode" toggle switch and a small icon. Below the navigation bar, the main content area has a white background. On the left, the heading "Welcome to PyArg!" is displayed in a large, dark font. Below this heading, there is a paragraph of text: "This is a Python package and web interface for solving various computational argumentation." followed by another line: "If you have any questions, feedback or ambitions to contribute, please contact [Daphne Odekerken \(D.Odekerken@UU.nl\)](mailto:D.Odekerken@UU.nl)." Below this text, the section "Contributors:" is followed by a bulleted list of names: [Matti Berthold](#), [AnneMarie Borg](#), [Jonas Klein](#), [Bertram Ludäscher](#), [Daphne Odekerken](#), and [Yilin Xia](#). On the right side of the main content area, there is a vertical blue sidebar with a menu. The menu items are "Abstract", "ASPIc+", "ABA", and "IAF". The "Abstract" item is currently selected, highlighted in a darker blue.

## Visualisation of abstract argumentation frameworks

The screenshot displays the PyArg web interface for visualising an Abstract Argumentation Framework (AF). The interface is divided into two main sections: the AF configuration and the visualisation.

**Abstract Argumentation Framework Configuration:**

- Buttons:** "Generate random" and "Open existing AF".
- Arguments:** A list containing "A", "B", and "C".
- Attacks:** A list containing "(A,B)", "(B,C)", "(C,B)", and "(B,A)".
- Download:** A button to download the AF, with a filename field containing "edited\_af" and a format dropdown set to "JSON".
- Evaluation:** A dropdown menu.

**Visualisation:**

- Default visualisation:** Shows a directed graph with three nodes: A, B, and C. The edges represent attacks: A attacks B, B attacks C, C attacks B, and B attacks A.
- Layered visualisation:** A tab for a more detailed visualisation.

## Visualisation of abstract argumentation frameworks

Abstract Argumentation Framework ⌵

Evaluation ⌵

**Semantics** Complete ⌵

**Evaluation strategy** Credulous ⌵

**The extension(s):**  
{} {B} {A, C}

**The accepted argument(s):**  
A B C

Click on the extension/argument buttons to display the corresponding argument(s) in the graph.

Explanation ⌵

Default visualisation Layered visualisation

```
graph LR; A((A)) --> B((B)); B((B)) --> A((A)); B((B)) --> C((C)); C((C)) --> B((B));
```

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Abstract Argumentation Framework ∨

Evaluation ∧

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Explanation ∨

Default visualisation Layered visualisation

```
graph LR; A((A)) -- red --> B((B)); B((B)) -- green --> C((C)); C((C)) -- red --> B((B)); B((B)) -- green --> A((A))
```



## Visualisation of abstract argumentation frameworks

Abstract Argumentation Framework ⌵

Evaluation ⌴

**Semantics** Complete ⌵

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```

# Computational Complexity

- Reasoning with AFs is generally hard

Problem	Grounded	Stable	Preferred	Complete
$\sigma$ -Exist	Trivial	NP-c	Trivial	Trivial
$\sigma$ -Exist <sup>NT</sup>	L	NP-c	NP-c	NP-c
$\sigma$ -Verif	P-c	L	coNP-c	L
$\sigma$ -Cred	P-c	NP-c	NP-c	NP-c
$\sigma$ -Skep	P-c	coNP-c	$\Pi_2^P$ -c	P-c

- $\sigma$ -Exist: Given  $F$ , is  $\sigma(F) \neq \emptyset$ ?
- $\sigma$ -Exist<sup>NT</sup>: Given  $F$ , is  $\sigma(F) \neq \emptyset$  s.t.  $F$  has at least one non-empty extension?
- $\sigma$ -Verif: Given  $F$  and  $S$ , is  $S \in \sigma(F)$ ?
- $\sigma$ -Cred: Given  $F$  and  $a$ , is  $a \in cred_\sigma(F)$ ?
- $\sigma$ -Skep: Given  $F$  and  $a$ , is  $a \in skep_\sigma(F)$ ?

W. Dvorák, P. E.Dunne: Computational Problems in Formal Argumentation and their Complexity. Handbook of Formal Argumentation: 631–688 (2018)

Approach proposed in (Besnard and Doutre 04). Intuition:

- Encoding arguments' acceptance in Boolean variables
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## Logical Encoding of Stable Semantics

For  $F = \langle A, R \rangle$ ,  $S \subseteq A$  is a stable extension of  $F$  iff  $S$  is a model of

$$\phi_{st}(F) = \bigwedge_{a \in A} (a \leftrightarrow \bigwedge_{(b,a) \in R} \neg b)$$

Similar encodings exist for conflict-freeness, admissibility and the complete semantics.

P. Besnard, S. Doutre: Checking the acceptability of a set of arguments. NMR 2004: 59-64

- For  $\sigma \in \{cf, ad, co, st\}$ ,  $\text{mod}(\phi_\sigma(F)) = \sigma(F)$ 
  - Compute one/each extension = compute one/each model
  - Decide the credulous acceptability of  $a$  = check if  $\phi_\sigma(F) \wedge a$  is SAT
  - Decide the skeptical acceptability of  $a$  = check if  $\phi_\sigma(F) \wedge \neg a$  is UNSAT
- For  $\sigma = gr$ , computation is polynomial (can be done with unit propagation over  $\phi_{co}(F)$ )
- For  $\sigma = pr$ , need to use other techniques, e.g. CEGAR or MSS extraction

- Since 2015, the International Competition on Computational Models of Argumentation (ICCMA) evaluates the best solvers for argumentation problems
  - <https://argumentationcompetition.org>
  - Many available solvers
- $\mu$ -toskia: in C++
  - Winner of ICCMA 2019
  - <https://bitbucket.org/andreasniskanen/mu-toksia/src/master/>
- Crustabri: in Rust
  - Winner of several tracks at ICCMA 2023 (9 sub-tracks over 13 in the main track, and 3 sub-tracks over 3 in the dynamic track)
  - <https://www.cril.univ-artois.fr/software/crustabri/>
- pygarg : not an ICCMA solver, open-source Python implementation of the SAT-based algorithms from Crustabri
  - `pip install pygarg`
  - <https://github.com/jgmailly/pygarg>

Andreas Niskanen, Matti Järvisalo:  $\mu$ -toskia: An Efficient Abstract Argumentation Reasoner. KR 2020: 800-804

J.-M. Lagniez, E. Lonca, J.-G. Maily: A SAT-based Approach for Argumentation Dynamics. AAMAS 2024

J.-G. Maily: pygarg: A Python engine for argumentation. Argument. Comput. 2024

If you like challenges, ICCMA 2025 will be announced soon (Sep. 17th, during SAFA 2024), and participation is open to everyone :)

`http://safa2024.argumentationcompetition.org`

`https://argumentationcompetition.org/2025/index.html`

## Using Pygarg (1)

- Remember: installation with `pip install pygarg`

Parsers for standard file formats are provided

```
import pygarg.dung.apx_parser
import pygarg.dung.dimacs_parser
```

```
args, atts = pygarg.dung.apx_parser.parse("test.apx")
args2, atts2 = pygarg.dung.dimacs_parser.parse("test.dimacs")
```



```
p af 2
1 2
```

```
arg(a1).
arg(a2).
att(a1,a2).
```

You can also declare the list of arguments and the list of attacks directly:

```
args3 = ["a1", "a2"]
atts3 = [["a1", "a2"]]
```



## Using Pygarg (2)

All interesting functions are in `pygarg.dung.solver`

- `credulous_acceptability(args, atts, argname, sem)`
- `skeptical_acceptability(args, atts, argname, sem)`
- `compute_some_extension(args, atts, sem)`
- `extension_enumeration(args, atts, sem)`
- `extension_counting(args, atts, sem)`

where `sem` is in `['CF', 'AD', 'ST', 'CO', 'PR', 'GR', 'ID', 'SST']`

Example:

```
from pygarg.dung import solver as solver
from pygarg.dung import apx_parser as parser

args, atts = parser.parse("test.apx")
print(solver.extension_enumeration(args, atts, 'CO'))

prints [['a1']]
```

## Two Aspects of Argumentation Dynamics

- Dynamic re-computation when an update occurs: when some arguments/attacks are added/deleted, can we re-compute the acceptability of arguments without running (naively) algorithms from scratch?

$$\left. \begin{array}{l} F = \langle A, R \rangle \\ \text{Acceptability of } a \in A \\ \text{New argument } x \\ \text{and attacks } R' \text{ from } x \end{array} \right\} \implies \text{Acceptability of } a \text{ in } F' = \langle A \cup \{x\}, R \cup R' \rangle$$

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- Belief change/strategic aspect: How to change (minimally?) an AF in order to satisfy some property (e.g. regarding arguments acceptability)

$$\left. \begin{array}{l} F = \langle A, R \rangle \\ \text{Constraint} \end{array} \right\} \implies F' = \langle A', R' \rangle \text{ which satisfies the constraint}$$

Introduction to Abstract Argumentation

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SAT-based Computation for Argumentation

What is Argumentation Dynamics?

Dynamic Computation

The Subgraph-based Approach

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Extension Enforcement

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Argumentation under Uncertainty

Argumentation Dynamics under Uncertainty

Application to a Multi-Agent Scenario: Automated Negotiation

Conclusion

## Two main approaches

- When an AF is updated (addition/deletion of arguments/attacks), can we re-compute the acceptability of arguments without re-starting from scratch?
- Two approaches in the literature:
  - Identify the part of the graph which is impacted by the update, and re-compute only for this (smaller) part
  - Use incremental SAT solving to keep track of what the SAT solver has learnt in previous computation steps

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# The Subgraph-based Approach: Algorithm

## Input:

- AF  $F_0 = \langle A_0, R_0 \rangle$
- Attack update  $u = \star(a, b)$ ,  $\star \in \{+, -\}$
- Semantics  $\sigma$
- Extension  $E_0 \in \sigma(F_0)$

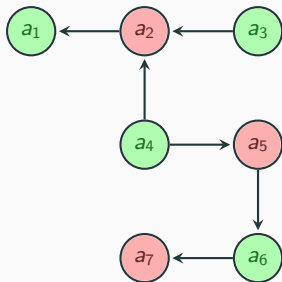
## Functions used:

- $I(u, A_0, E_0)$  returns the set of arguments influenced by the update
- $R(U, A_0, E_0)$  returns the reduced AF
- $solve_\sigma(F)$  returns a  $\sigma$ -extension of an AF  $F$  if it exists,  $\perp$  otherwise

```
 $S = I(u, A_0, E_0)$   
if  $S = \emptyset$  then  
    return  $E_0$   
else  
     $F_1 = R(u, A_0, E_0)$   
     $E_1 = solve_\sigma(F_1)$   
    if  $E_1 \neq \perp$  then  
        return  $(E_0 \setminus S) \cup E_1$   
    else  
        return  $solve_\sigma(u(A_0))$   
    end if  
end if
```

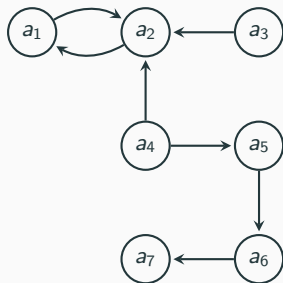
Gianvincenzo Alfano, Sergio Greco, Francesco Parisi: Efficient Computation of Extensions for Dynamic Abstract Argumentation Frameworks: An Incremental Approach. IJCAI 2017: 49-55

## The Subgraph-based Approach: Example



- $F_0 = \langle A, R \rangle$ ,  $\sigma = st$ ,  
 $E_0 = \{a_1, a_3, a_4, a_6\}$

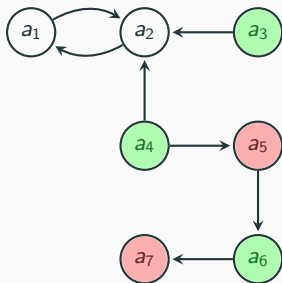
## The Subgraph-based Approach: Example



- $F_0 = \langle A, R \rangle$ ,  $\sigma = st$ ,  
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- $u = +(a_1, a_2)$

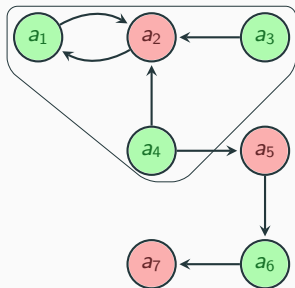


## The Subgraph-based Approach: Example



- $F_0 = \langle A, R \rangle$ ,  $\sigma = st$ ,  
 $E_0 = \{a_1, a_3, a_4, a_6\}$
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- Influenced set  
 $I(u, A_0, E_0) = \{a_1, a_2\}$

## The Subgraph-based Approach: Example

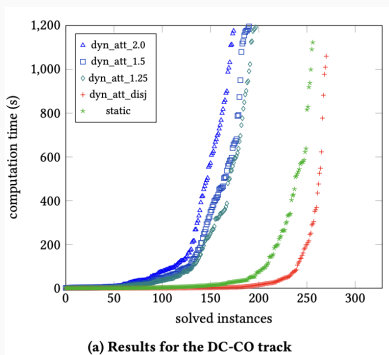


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- Influenced set  
 $I(u, A_0, E_0) = \{a_1, a_2\}$
- Re-computation is localized to a smaller graph  $R(U, A_0, E_0)$

- **In structured argumentation:** Gianvincenzo Alfano, Sergio Greco, Francesco Parisi, Gerardo Ignacio Simari, Guillermo Ricardo Simari: An Incremental Approach to Structured Argumentation over Dynamic Knowledge Bases. KR 2018: 78-87
- **In bipolar AFs:** Gianvincenzo Alfano, Sergio Greco, Francesco Parisi: A meta-argumentation approach for the efficient computation of stable and preferred extensions in dynamic bipolar argumentation frameworks. *Intelligenza Artificiale* 12(2): 193-211 (2018)
- **For arguments skeptical acceptability:** Gianvincenzo Alfano, Sergio Greco, Francesco Parisi: An Efficient Algorithm for Skeptical Preferred Acceptance in Dynamic Argumentation Frameworks. IJCAI 2019: 18-24
- **In higher-order bipolar AFs:** Gianvincenzo Alfano, Andrea Cohen, Sebastian Gottifredi, Sergio Greco, Francesco Parisi, Guillermo Ricardo Simari: Credulous acceptance in high-order argumentation frameworks with necessities: An incremental approach. *Artif. Intell.* 333: 104159 (2024)

# Incremental SAT-based Computation

- Incremental SAT-based approach implemented in Crustabri, won all sub-tracks of the dynamic track at ICCMA 2023
- Idea: use the assumption mechanism of SAT solvers over variables representing the disjunction of attackers. Allows to easily update the set of attacks and the set of arguments



- Red: Crustabri approach
- Green: re-computation from scratch
- Blue: various versions of  $\mu$ -toksia approach

- Future work: combine our approach with “subgraph-based” approach

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Conclusion

$$\left. \begin{array}{l} F = \langle A, R \rangle \\ E \subseteq A \\ \text{should be (part of)} \\ \text{an extension} \end{array} \right\} \Rightarrow F' = \langle A', R' \rangle \text{ with } E \\ \text{(part of) an extension}$$

### Different approaches

- (Baumann and Brewka) No change of the existing attacks, new arguments and attacks can be added
- (Coste-Marquis et al) The existing attacks can be modified
- (Doutre and Maily) The semantics can be modified

R. Baumann, G. Brewka: Expanding Argumentation Frameworks: Enforcing and Monotonicity Results. COMMA 2010: 75-86

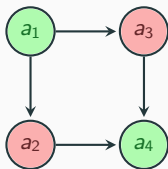
S. Coste-Marquis, S. Konieczny, J.-G. Maily, P. Marquis: Extension Enforcement in Abstract Argumentation as an Optimization Problem. IJCAI 2015: 2876-2882

S. Doutre, J.-G. Maily: Semantic Change and Extension Enforcement in Abstract Argumentation. SUM 2017: 194-207

# Example of Strong Enforcement

R. Baumann, G. Brewka: Expanding Argumentation Frameworks: Enforcing and Monotonicity Results. COMMA 2010: 75-86

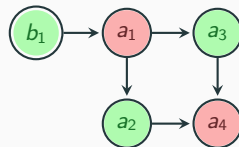
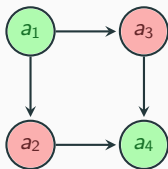
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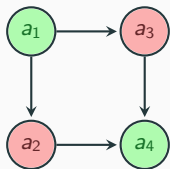




## Example of Argument-fixed Enforcement

S. Coste-Marquis, S. Konieczny, J.-G. Maily, P. Marquis: Extension Enforcement in Abstract Argumentation as an Optimization Problem. IJCAI 2015: 2876-2882

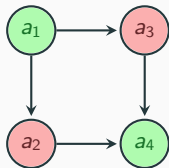
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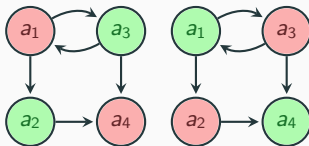
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- How to enforce  $E = \{a_2, a_3\}$  in  $F$ ?



Two extensions:



- Example: stable semantics
- Idea: generalize the propositional encoding to take into account the attack relation

$$\phi_{st}(F) = \bigwedge_{a \in A} (a \leftrightarrow \bigwedge_{(b,a) \in R} \neg b)$$

$$\phi'_{st}(A) = \bigwedge_{a \in A} (acc_a \leftrightarrow \bigwedge_{b \in A} (att_{b,a} \rightarrow \neg acc_b))$$

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- If  $F = \langle A, R \rangle$  is known,  $\phi'_{st}(A) \wedge \bigwedge_{(a,b) \in R} att_{a,b} \wedge \bigwedge_{(a,b) \notin R} \neg att_{a,b}$  corresponds to  $\phi_{st}(F)$

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- To enforce,  $E \subseteq A$ , search a model of  $\phi'_{st}(A) \wedge \bigwedge_{a \in E} acc_a \wedge \bigwedge_{a \notin E} \neg acc_a$ : the values of the  $att_{a,b}$  variables correspond to an AF

S. Coste-Marquis, S. Konieczny, J.-G. Mailly, P. Marquis: Extension Enforcement in Abstract Argumentation as an Optimization Problem. IJCAI 2015: 2876-2882

$F = \langle A, R \rangle$   
 $E \subseteq A$   
should be (part of)  
an extension

$\Rightarrow$

$F' = \langle A', R' \rangle$  with  $E$   
(part of) an extension and  
 $F'$  as close as possible to  $F$

$$\left. \begin{array}{l} F = \langle A, R \rangle \\ E \subseteq A \\ \text{should be (part of)} \\ \text{an extension} \end{array} \right\} \Rightarrow \begin{array}{l} F' = \langle A', R' \rangle \text{ with } E \\ \text{(part of) an extension and} \\ F' \text{ as close as possible to } F \end{array}$$

- (Coste-Marquis et al) translate the SAT encoding in pseudo-Boolean constraints, optimize w.r.t. an objective function (distance between  $F$  and  $F'$ )

S. Coste-Marquis, S. Konieczny, J.-G. Mailly, P. Marquis: Extension Enforcement in Abstract Argumentation as an Optimization Problem. IJCAI 2015: 2876-2882

$$\left. \begin{array}{l} F = \langle A, R \rangle \\ E \subseteq A \\ \text{should be (part of)} \\ \text{an extension} \end{array} \right\} \implies \begin{array}{l} F' = \langle A', R' \rangle \text{ with } E \\ \text{(part of) an extension and} \\ F' \text{ as close as possible to } F \end{array}$$

- (Coste-Marquis et al) translate the SAT encoding in pseudo-Boolean constraints, optimize w.r.t. an objective function (distance between  $F$  and  $F'$ )
- (Wallner et al) translate into partial MaxSAT: the SAT encoding of enforcement corresponds to hard clauses, and unit clauses corresponding to the  $att_{a,b}$  variables correspond to the soft clauses. CEGAR algorithm for second level of the polynomial hierarchy
  - Available software:  
<https://bitbucket.org/andreasniskanen/pakota/src/master/>
- Scalability: up to 350 arguments for NP-complete problems, 200 arguments for  $\Sigma_2^P$ -complete problems ( $\simeq 10$  seconds for most instances)

S. Coste-Marquis, S. Konieczny, J.-G. Maily, P. Marquis: Extension Enforcement in Abstract Argumentation as an Optimization Problem. IJCAI 2015: 2876-2882

J. P. Wallner, A. Niskanen, M. Järvisalo: Complexity Results and Algorithms for Extension Enforcement in Abstract Argumentation. J. Artif. Intell. Res. 60: 1-40 (2017)



### More information about enforcement and related topics:

- **Status enforcement:** A. Niskanen, J. P. Wallner, M. Järvisalo: Optimal Status Enforcement in Abstract Argumentation. IJCAI 2016: 1216-1222
- **Belief change in argumentation:**
  - S. Coste-Marquis, S. Konieczny, J.-G. Maily, P. Marquis: On the Revision of Argumentation Systems: Minimal Change of Arguments Statuses. KR 2014
  - S. Coste-Marquis, S. Konieczny, J.-G. Maily, P. Marquis: A Translation-Based Approach for Revision of Argumentation Frameworks. JELIA 2014: 397-411
  - M. Diller, A. Haret, T. Linsbichler, S. Rümmele, S. Woltran: An extension-based approach to belief revision in abstract argumentation. Int. J. Approx. Reason. 93: 395-423 (2018)
  - S. Doutre, A. Herzig, L. Perrussel: A Dynamic Logic Framework for Abstract Argumentation. KR 2014

### Two survey papers

- S. Doutre, J.-G. Maily: Constraints and changes: A survey of abstract argumentation dynamics. Argument Comput. 9(3): 223-248 (2018)
- R. Baumann, S. Doutre, J.-G. Maily, J. P. Wallner, Enforcement in Formal Argumentation, in Handbook of Formal Argumentation (Vol.2) (2021)

# Incomplete Argumentation Framework (IAF)

$I = \langle A, A^?, R, R^? \rangle$  where

- $A, A^?$  are disjoint sets of arguments
- $R, R^?$  are disjoint sets of attacks over  $A \cup A^?$

such that

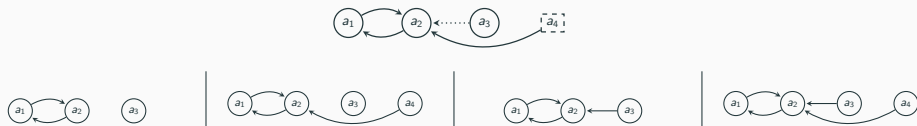
- $A, R$  are certain arguments and attacks
- $A^?, R^?$  are uncertain arguments and attacks



J.-G. Maily: Yes, no, maybe, I don't know: Complexity and application of abstract argumentation with incomplete knowledge. *Argument Comput.* 13(3): 291-324 (2022)

# Completions of an IAF

Completions = AFs compatible with the incomplete knowledge encoded in the IAF  
 $\simeq$  possible worlds



# Possible and Necessary Reasoning

- Possible reasoning: some property is true for some completion of the IAF
- Necessary reasoning: some property is true for each completion of the IAF



D. Baumeister, M. Järvisalo, D. Neugebauer, A. Niskanen, J. Rothe: Acceptance in incomplete argumentation frameworks. *Artif. Intell.* 295: 103470 (2021)

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- $a_3$  is skeptically accepted in each completion  $\rightarrow$  necessarily skeptically accepted

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- $a_2$  is credulously accepted in some completion  $\rightarrow$  possibly credulously accepted

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- $a_1$  is credulously accepted in each completion  $\rightarrow$  necessarily credulously accepted

D. Baumeister, M. Järvisalo, D. Neugebauer, A. Niskanen, J. Rothe: Acceptance in incomplete argumentation frameworks. *Artif. Intell.* 295: 103470 (2021)



# Complexity of Reasoning with IAFs

- Possible Credulous Acceptability:  $a$  is in some extension of some completion
- Possible Skeptical Acceptability:  $a$  is in each extension of some completion
- Possible Verification:  $S$  is an extension of some completion
- Necessary Credulous Acceptability:  $a$  is in some extension of each completion
- Necessary Skeptical Acceptability:  $a$  is in each extension of each completion
- Necessary Verification:  $S$  is an extension of each completion

Semantics	PCA	PSA	PV	NCA	NSA	NV
<b>ad</b>	NP-c	trivial	NP-c	$\Pi_2^P$ -c	trivial	P
<b>st</b>	NP-c	$\Sigma_2^P$ -c	NP-c	$\Pi_2^P$ -c	coNP-c	P
<b>co</b>	NP-c	NP-c	NP-c	$\Pi_2^P$ -c	coNP-c	P
<b>gr</b>	NP-c	NP-c	NP-c	coNP-c	coNP-c	P
<b>pr</b>	NP-c	$\Sigma_3^P$ -c	$\Sigma_2^P$ -c	$\Pi_2^P$ -c	$\Pi_2^P$ -c	coNP-c

- SAT-based algorithms, CEGAR for second/third level of PH

A CAF is an argumentation framework where arguments are divided in three parts: *fixed*, *uncertain* and *control*.

**fixed** background knowledge about a static environment

**uncertain** changes that may occur in the environment

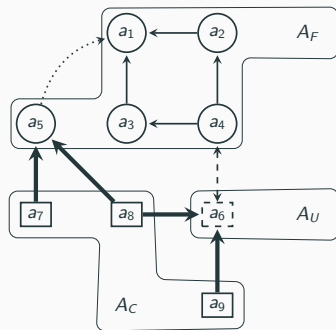
**control** possible actions of the agent

CAFs generalize IAFs in two directions:

- a new kind of uncertainty about the direction of attacks
- the control part representing how the agent can react to uncertain “threats”

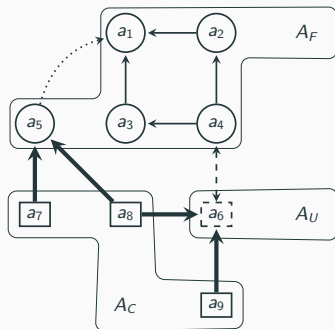
Y. Dimopoulos, [J.-G. Maily](#), P. Moraitis: Control Argumentation Frameworks. AAAI 2018: 4678-4685

# A Picture is Worth a Thousand Words



- Fixed part: circle arguments + plain arrows
- Uncertain part:
  - dashed arguments
  - dotted arrows
  - two-heads dashed arrows
- Control part: square arguments + bold arrows

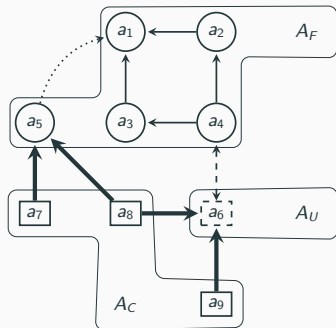
# A Picture is Worth a Thousand Words



- certain knowledge: always exist

- Fixed part: circle arguments + plain arrows
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  - dotted arrows
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- Control part: square arguments + bold arrows

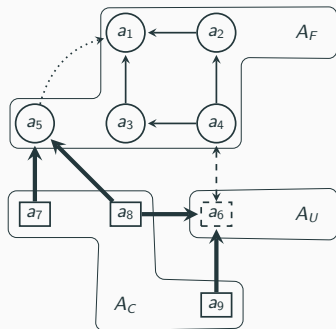
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- Fixed part: circle arguments + plain arrows
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  - dotted arrows
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- Control part: square arguments + bold arrows

- the argument could exist, or not

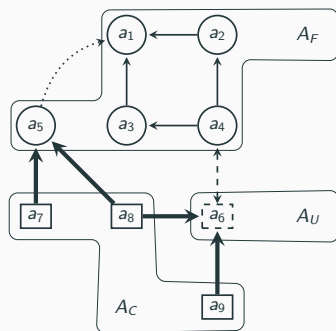
# A Picture is Worth a Thousand Words



- the attack could exist, or not

- Fixed part: circle arguments + plain arrows
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- Control part: square arguments + bold arrows

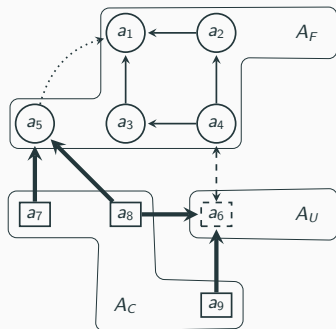
# A Picture is Worth a Thousand Words



- Fixed part: circle arguments + plain arrows
- Uncertain part:
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- Control part: square arguments + bold arrows

- the attack exists (if both arguments exist), but we are not sure of the direction

# A Picture is Worth a Thousand Words



- Fixed part: circle arguments + plain arrows
- Uncertain part:
  - dashed arguments
  - dotted arrows
  - two-heads dashed arrows
- Control part: **square arguments + bold arrows**

- exist only if the agent selects the arguments

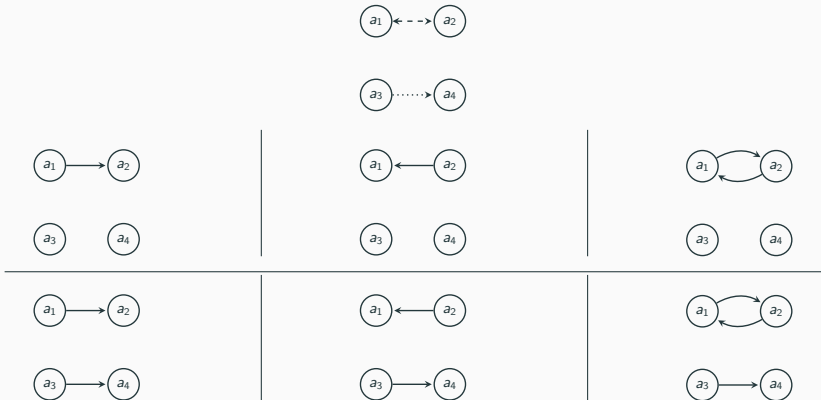


- Generalizes the notion of completion from IAFs, with 3 possible options for each “unknown direction conflict”



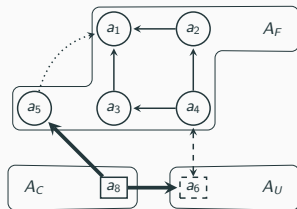
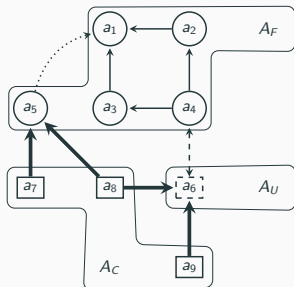
# Completion

- Generalizes the notion of completion from IAFs, with 3 possible options for each “unknown direction conflict”



# Control Configuration

- A control configuration is a subset  $cc \subseteq A_C$
- A configured CAF: remove from the initial CAF the arguments  $A_C \setminus cc$  (and their attacks)



Example: In the CAF configured by  $cc = \{a_8\}$ ,  $T = \{a_1\}$  is accepted whatever the completion

## Formal Definition of Controllability

Given

- a target  $T \subseteq A_F$
- a semantics  $\sigma$

CAF is skeptically (resp. credulously) *controllable* w.r.t.  $T$  and  $\sigma$  if  $\exists cc \subseteq A_C$   
s.t.

- CAF' is the result of configuring CAF by  $cc$
- $T$  is included in every (resp. some)  $\sigma$ -extension of every completion of CAF'

Y. Dimopoulos, [J.-G. Maily](#), P. Moraitis: Control Argumentation Frameworks. AAAI 2018: 4678-4685

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Y. Dimopoulos, [J.-G. Maily](#), P. Moraitis: Control Argumentation Frameworks. AAAI 2018: 4678-4685

- Possible controllability: replace “every completion” by “some completion”

[J.-G. Maily](#): Possible Controllability of Control Argumentation Frameworks. COMMA 2020: 283-294

	Possible		Necessary	
	Skeptical	Credulous	Skeptical	Credulous
Grounded	NP-c	NP-c	$\Sigma_2^P$ -c	$\Sigma_2^P$ -c
Complete	NP-c	NP-c	$\Sigma_2^P$ -c	$\Sigma_3^P$ -c
Stable	$\Sigma_2^P$ -c	NP-c	$\Sigma_2^P$ -c	$\Sigma_3^P$ -c
Preferred	$\Sigma_3^P$ -c	NP-c	$\Sigma_3^P$ -c	$\Sigma_3^P$ -c

- QBF encodings proposed in (Dimopoulos et al, Maily)
- CEGAR algorithms proposed in (Niskanen et al)

Y. Dimopoulos, J.-G. Maily, P. Moraitis: Control Argumentation Frameworks. AAI 2018: 4678-4685

J.-G. Maily: Possible Controllability of Control Argumentation Frameworks. COMMA 2020: 283-294

A. Niskanen, D. Neugebauer, M. Järvisalo: Controllability of Control Argumentation Frameworks. IJCAI 2020: 1855-1861

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Conclusion

- Context: several agents have their own knowledge/beliefs, preferences and goals
- Objective: reach an agreement between them (e.g. about an action to perform, a product to buy, some allocation of resources/tasks, etc)
- Example:
  - The car seller knows the different cars and their features, and wants to sell the most expensive one
  - The potential buyer knows his needs (small car, family car, big trunk, . . . ) and preferences (color of the car, heating seats, . . . ), and wants to buy a car that meets these needs, as cheap as possible



- Argumentation: activity that aims at increasing (or decreasing) the acceptance degree of a controversial point of view
- Arguments: pieces of information that justify (or defeat) a point of view
- Using argumentation in negotiation improves the chances to reach an agreement (Sycara 1990)
  - An offer supported by a good argument is more likely to be accepted
  - An agent can modify its goals and preferences when he receives arguments

K. Sycara: Persuasive argumentation in negotiation. *Theory and Decision* 28(3):203-242, 1990.

- If available, opponent modeling is a great tool to improve the issue of negotiation
  - possibility to choose offers/arguments that the opponent is likely to accept
  - anticipate what he will say
  - use his own arguments to convince him
- CAFs are a good way to model the knowledge of an agent about the other agent
  - Fixed part: certain knowledge about the opponent
  - Uncertain part: uncertain knowledge about the opponent
  - Control part: possible actions of the agent to convince the opponent

Y. Dimopoulos, J.-G. Maily, Pavlos Moraitis: Arguing and negotiating using incomplete negotiators profiles.

Auton. Agents Multi Agent Syst. 35(2): 18 (2021)

- No fixed role: both agents act as proponent and opponent in turn
- Each agent has a (incomplete and uncertain) representation of its opponent's theory: fixed and uncertain part of the CAF
- In the CAF, control arguments come from the agent's own theory: persuasive arguments
- The proponent selects the best offer w.r.t. his own theory, but uses arguments from the opponent's theory to defend the offer → facilitates persuasion

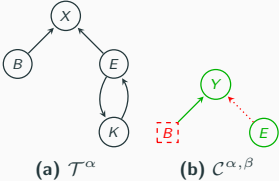
Y. Dimopoulos, J.-G. Mailly, Pavlos Moraitis: Arguing and negotiating using incomplete negotiators profiles. *Auton. Agents Multi Agent Syst.* 35(2): 18 (2021)

Negotiation theory of an agent  $\alpha$ :  $\mathcal{T} = \langle \mathcal{O}, \mathcal{T}^\alpha, \mathcal{C}^{\alpha,\beta}, \mathcal{F}^\alpha \rangle$  with

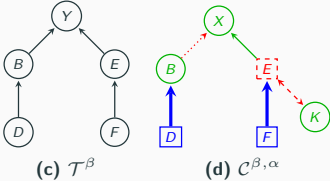
- $\mathcal{O}$ : set of offers
  - Can be “simple” objects (mono-issue negotiation):  $\{car_1, car_2, \dots, car_n\}$
  - Or “complex” objects (multi-issue negotiation):  
 $\{(car_1, price_1, delivery_1), \dots, (car_n, price_m, delivery_k)\}$
- $\mathcal{T}^\alpha$ : the agent's AF
- $\mathcal{C}^{\alpha,\beta}$ : the knowledge of  $\alpha$  about his opponent  $\beta$ 
  - $\mathcal{C}^{\alpha,\beta}$  is made from  $\mathcal{T}^\beta$ : there is uncertainty, there is ignorance, but there is no mistake or lie
- $\mathcal{F}^\alpha : \mathcal{O} \rightarrow 2^{A_p^\alpha}$  maps offers to the set of practical arguments supporting them

# Example of Negotiation Theories

Agent  $\alpha$ :  $X$  supports  $O$

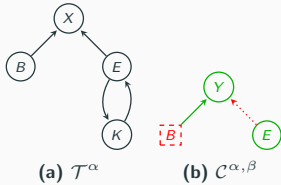


Agent  $\beta$ :  $Y$  supports  $O$

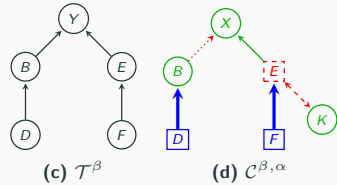


# Bidding Strategy

Agent  $\alpha$ :  $X$  supports  $O$



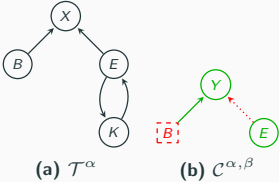
Agent  $\beta$ :  $Y$  supports  $O$



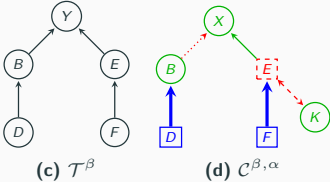
$\alpha$ 's turn:  $X$  is not accepted in  $\mathcal{T}^\alpha$ , so  $\alpha$  cannot support the (unique) offer  $O$   
→ the token goes to  $\beta$

# Bidding Strategy

Agent  $\alpha$ :  $X$  supports  $O$



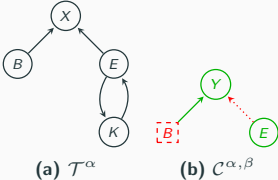
Agent  $\beta$ :  $Y$  supports  $O$



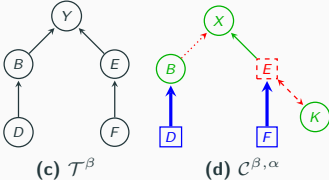
$\beta$ 's turn: best offer according to  $\beta$ 's personal AF is  $O$  because the supporting argument  $Y$  is accepted in  $\mathcal{T}^\beta$

# Bidding Strategy

Agent  $\alpha$ :  $X$  supports  $O$



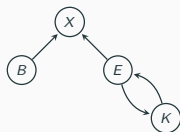
Agent  $\beta$ :  $Y$  supports  $O$



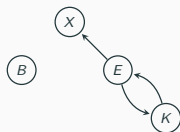
$\beta$ 's turn: support argument for  $O$  in  $\alpha$ 's theory is  $X$



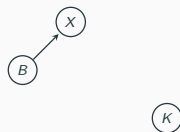
# $\beta$ 's Proposal without Control



(a) Completion 1



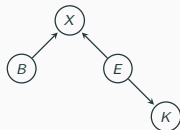
(b) Completion 2



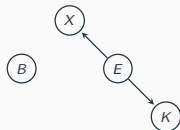
(c) Completion 3



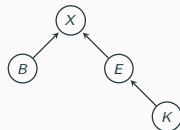
(d) Completion 4



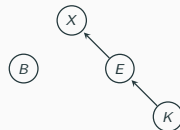
(e) Completion 5



(f) Completion 6



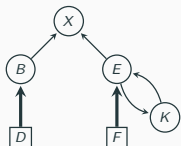
(g) Completion 7



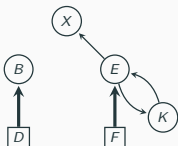
(h) Completion 8

- $X$  is not accepted in each completion (e.g. Completion 1)

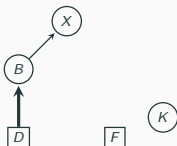
# $\beta$ 's Proposal with Control



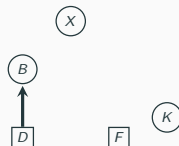
(a) Completion 1



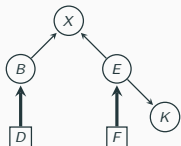
(b) Completion 2



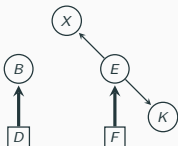
(c) Completion 3



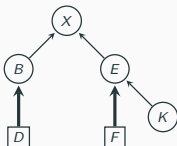
(d) Completion 4



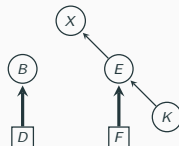
(e) Completion 5



(f) Completion 6



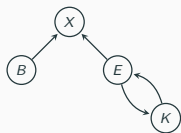
(g) Completion 7



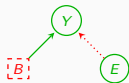
(h) Completion 8

- X is accepted in each completion

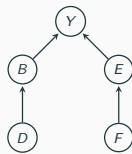
# Acceptance Strategy



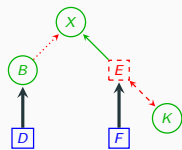
(a)  $T^\alpha$



(b)  $C^{\alpha,\beta}$



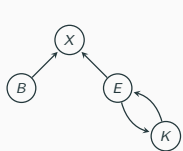
(c)  $T^\beta$



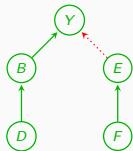
(d)  $C^{\beta,\alpha}$

$\beta$ 's turn: proposal is offer  $O$ , supported by argument  $X$ , defended by  $D$  and  $F$

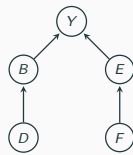
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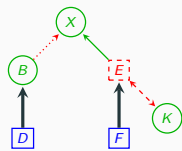
(a)  $T^\alpha$



(b)  $C^{\alpha, \beta}$



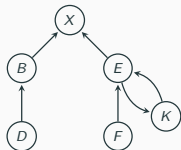
(c)  $T^\beta$



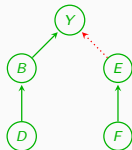
(d)  $C^{\beta, \alpha}$

$\alpha$  updates its CAF: uncertainty decreases

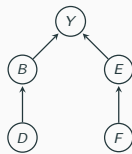
# Acceptance Strategy



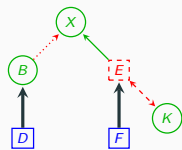
(a)  $T^\alpha$



(b)  $C^{\alpha,\beta}$



(c)  $T^\beta$



(d)  $C^{\beta,\alpha}$

$\alpha$  updates its own theory.  $X$  is now accepted: **agreement**

- If both agents end with no available offer, then the negotiation fails
- Otherwise, the outcome of the negotiation is the proponent's offer from the last round of the dialogue
- Experiments have shown the interest of using CAFs: better agreement rate if agents have enough information on their opponent and enough control arguments

Introduction to Abstract Argumentation

Dung's Framework

SAT-based Computation for Argumentation

What is Argumentation Dynamics?

Dynamic Computation

The Subgraph-based Approach

The Iterative SAT-based Approach

Extension Enforcement

How to modify arguments acceptability?

Argumentation under Uncertainty

Argumentation Dynamics under Uncertainty

Application to a Multi-Agent Scenario: Automated Negotiation

Conclusion

## Summary

- Argument-based reasoning is computationally hard, but can be solved thanks to SAT-based techniques and various algorithmic tricks (e.g. subgraph selection in dynamic argumentation)
- Argumentation under uncertainty/in dynamics scenarios has theoretical interest, and practical interest (e.g. automated negotiation)

## Future work

- Multi-issue negotiation: how can agent make concessions?
  - Work in progress with a PhD student
- Richer frameworks (supports, collective attacks, weighted, higher order relations, etc)
- Other kinds of semantics (ranking, gradual)
- Real world applications (e.g. online dispute resolution)



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Thanks for your attention!